

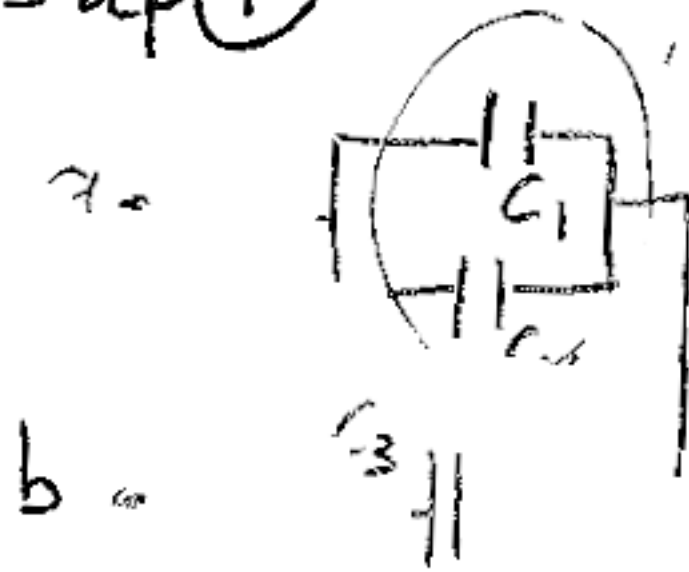
$$C_1 = 2.50 \mu\text{F} \quad q_1 = ? \quad V_1 = ?$$

$$C_2 = 4.60 \mu\text{F} \quad q_2 = ? \quad V_2 = ? \quad V_{ad} = ?$$

$$C_3 = 6.45 \mu\text{F} \quad q_3 = ? \quad V_3 = ?$$

I'll approach this by finding an equivalent capacitance between points a & b & then go backwards

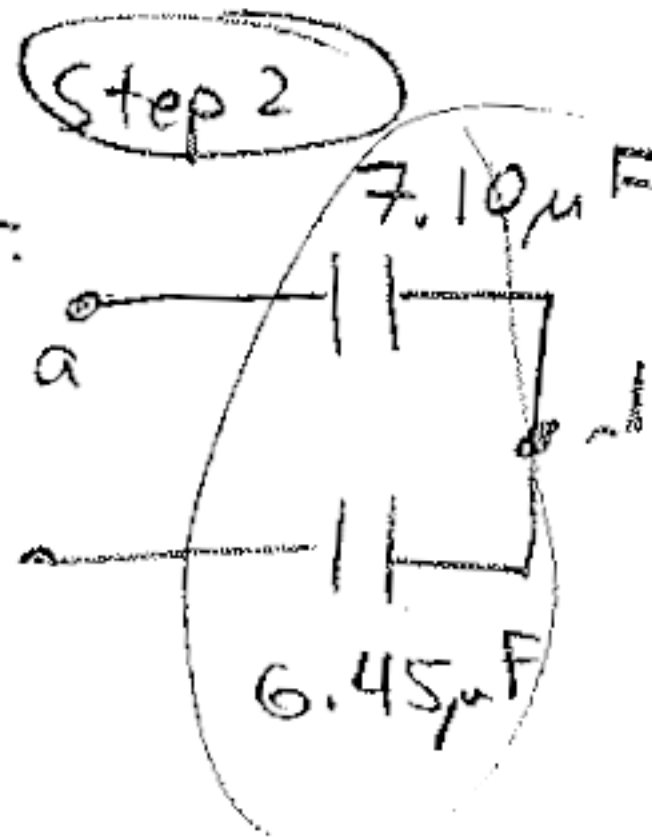
step 1



$$C_{\text{equiv}} = C_1 + C_2$$

$$= 2.50 \mu\text{F} + 4.60 \mu\text{F}$$

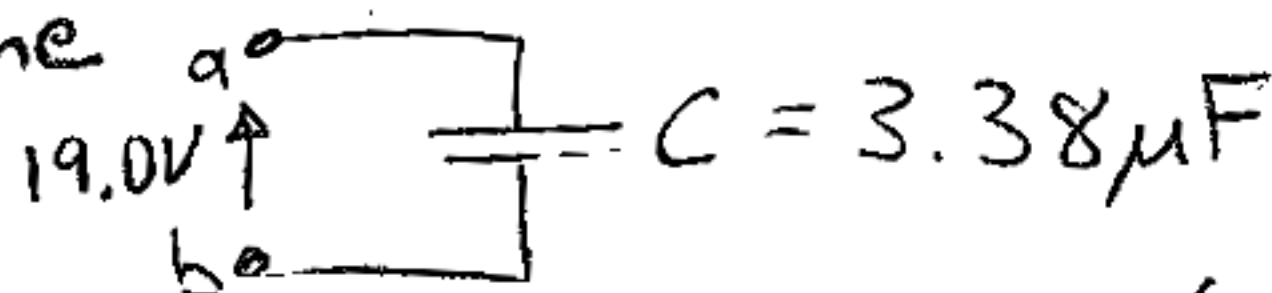
$$= 7.10 \mu\text{F}$$



$$\frac{1}{C_{\text{equiv}}} = \frac{1}{7.10 \mu\text{F}} + \frac{1}{6.45 \mu\text{F}}$$

$$C_{\text{equiv}} = 3.38 \mu\text{F}$$

So, if we replace all these capacitors with a single one



& the charge flowing from the battery =  $Q_{\text{tot}} = (19.0\text{V})(3.38 \times 10^{-6} \frac{\text{C}}{\text{V}})$   
 $= 6.42 \times 10^{-5} \text{C}$

If we think of this same  $Q$  in step 2 then there must be  $Q_{\text{tot}}$  on the  $6.45 \mu\text{F}$  &  $7.10 \mu\text{F}$  capacitor since they are in series so  $V$  across the  $6.45 \mu\text{F}$  capacitor =  $\frac{6.42 \times 10^{-5} \text{C}}{6.45 \times 10^{-6} \frac{\text{C}}{\text{V}}}$   
 $= 9.95 \text{V}$   
 so  $q_3 = 6.42 \times 10^{-5} \text{C}$   $V_3 = 9.95 \text{V}$

this means that the  $V_{ad} = 19.0\text{V} - 9.95\text{V} = 9.05\text{V}$

(check  $\frac{6.42 \times 10^{-5} \text{C}}{(7.10 \times 10^{-6} \frac{\text{C}}{\text{V}})} = 9.04 \text{V}$  (agree to last place))

now,  $V_{ad} = V_1 = V_2$  so we just need  $q_1$  &  $q_2$

check

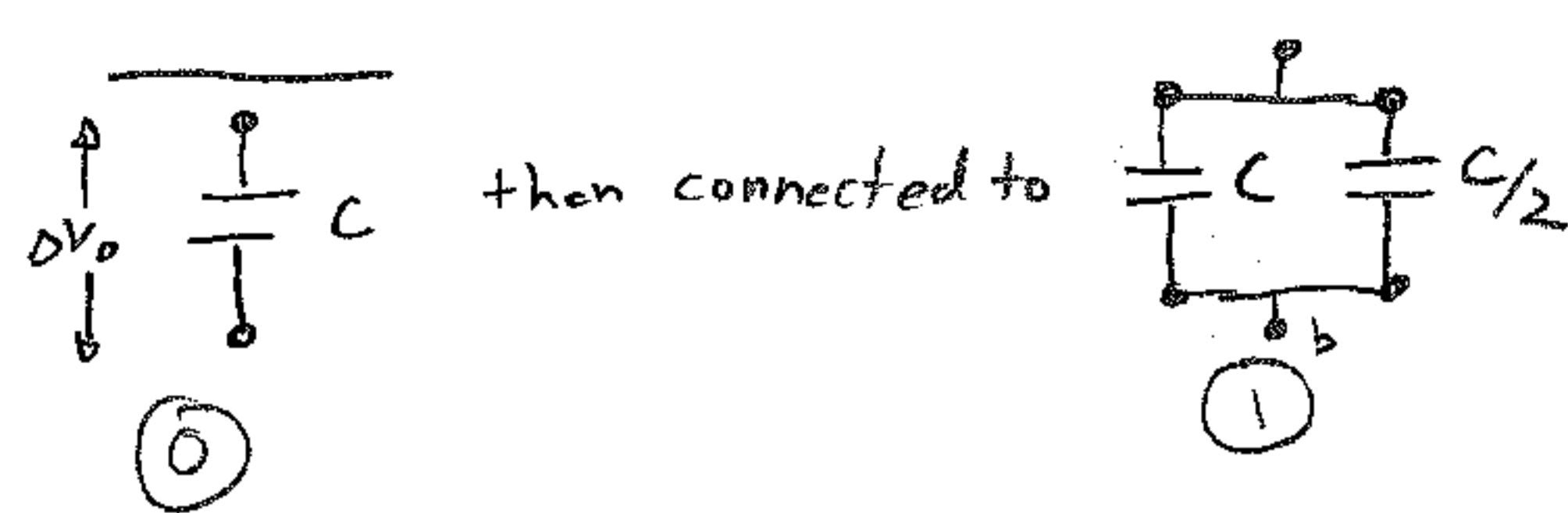
$$q_1 + q_2 = 64.2 \times 10^{-6} \text{C} \text{ ok!}$$

$$q_1 = (9.05\text{V})(2.50 \times 10^{-6} \frac{\text{C}}{\text{V}})$$

$$= 22.6 \times 10^{-6} \text{C}$$

$$q_2 = (9.05\text{V})(4.60 \times 10^{-6} \frac{\text{C}}{\text{V}})$$

$$= 41.6 \times 10^{-6} \text{C}$$



$Q_0 = ?$   
 $V_{ab} = ?$   
 $U_0 = ?$   
 $U_f = ?$   
 $\Delta U = ?$

Initially ① we have  $V_0$  across  $C$

or  $Q_0 = CV_0$  then, we

connect another capacitor as shown in ①

We know;

1) Charge is conserved  $\Rightarrow$

$$\begin{array}{r}
 Q \text{ on } C \text{ in } \textcircled{0} \\
 + q \text{ on } \frac{C}{2} \text{ in } \textcircled{1} \\
 \hline
 Q_0
 \end{array}$$

2)  $V_{ab} = V_{\text{across } C} = V_{\text{across } C/2}$

put it all together

$$CV_{ab} + \frac{C}{2}V_{ab} = Q_0 = \left(C + \frac{C}{2}\right)V_{ab}$$

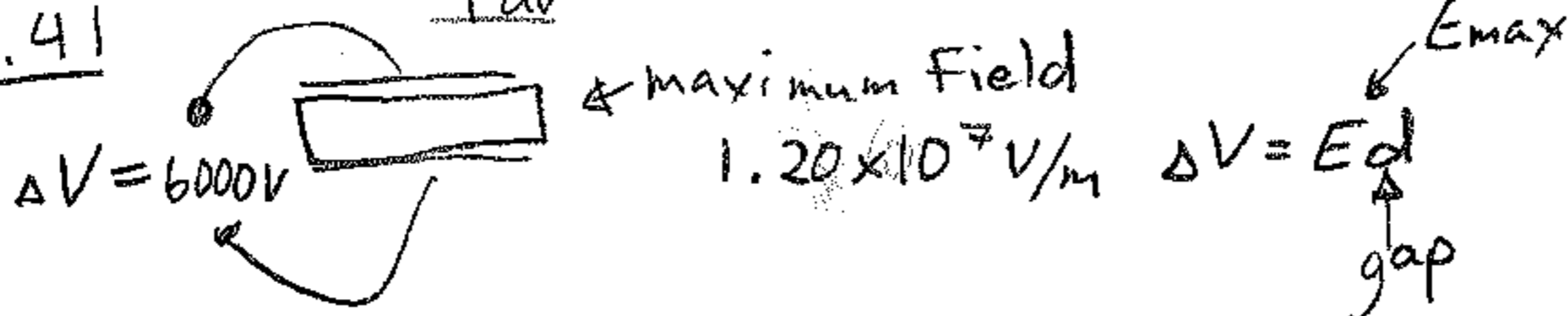
$$V_{ab} = Q_0 / \left(\frac{3}{2}C\right) = CV_0 / \left(\frac{3}{2}C\right) = \frac{2}{3}V_0$$

$$U_0 = \frac{1}{2}CV_0^2$$

$$U_{\textcircled{1}} = \frac{1}{2}C\left(\frac{2}{3}V_0\right)^2 + \frac{1}{2}\frac{C}{2}\left(\frac{2}{3}V_0\right)^2 = \left(\frac{2}{3}\right)\left(\frac{1}{2}CV_0^2\right)$$

$$\Delta U = \frac{1}{3}\left(\frac{1}{2}CV_0^2\right)$$

24.41



to minimize A, we want d as big as possible

$$d = \frac{\Delta V}{E_{max}} = \frac{6000V}{1.20 \times 10^7 V/m} = 5.00 \times 10^{-4} m$$

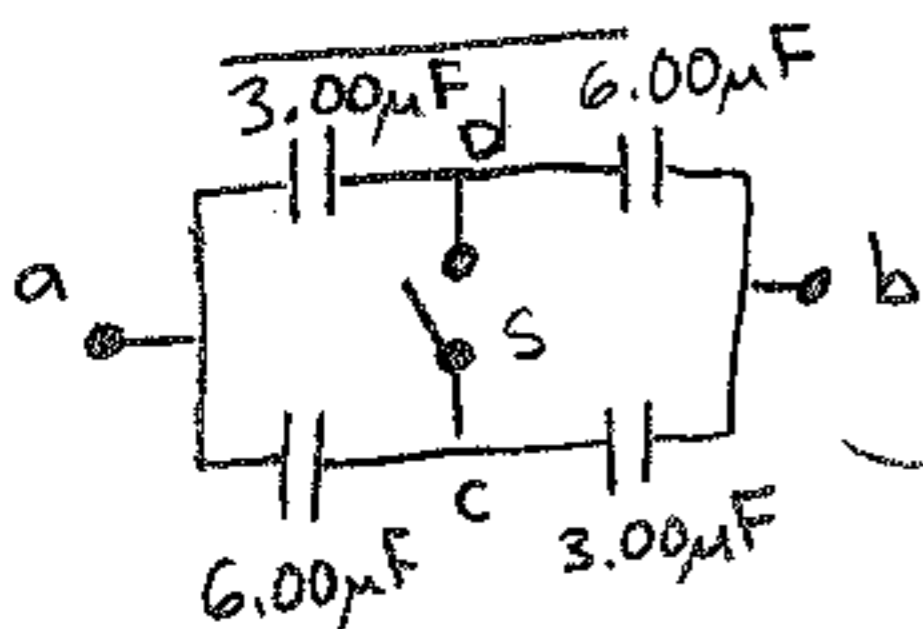
$$C = \frac{\epsilon_0 A}{d} = 1.10 \times 10^{-9} F \quad A \propto C$$

$$A = \frac{dC}{\epsilon_0} = \frac{(5.00 \times 10^{-4} m)(1.1 \times 10^{-9} \frac{C}{V})}{3.70 (8.85 \times 10^{-12} \frac{C}{Vm})}$$

$$= 0.0168 m$$

note: not a good idea to design right at the limit!

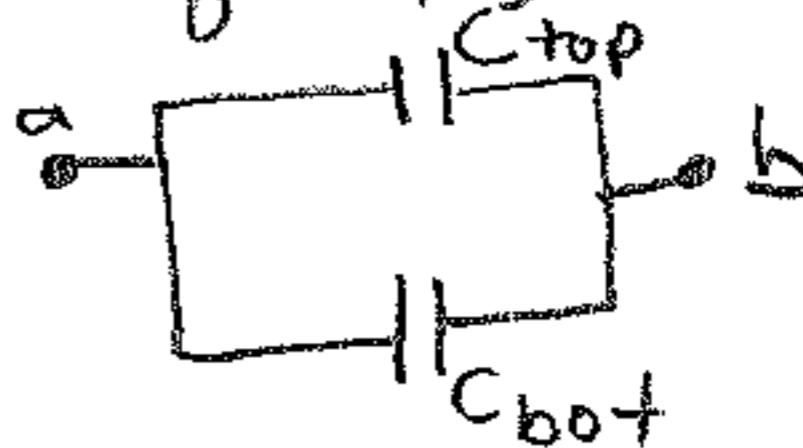
24.60



$$V_{ab} = 210V$$

$$V_{cd} = ?$$

Find equiv  $\epsilon$  go backwards



$$\frac{1}{C_{top}} = \frac{1}{3\mu F} + \frac{1}{6\mu F}$$

$$C_{top} = 2\mu F = C_{bot}$$

$$V_{top} = V_{bot}$$

$$Q_{top} = Q_{bot} \quad \text{since } V_{top} = V_{bot}$$

$$= (210V)(2\mu F)$$

$$= 4.2 \times 10^{-4} C$$

$$V_{ad} = \frac{4.20 \mu C}{3.00 \mu \frac{C}{V}} = 140V$$

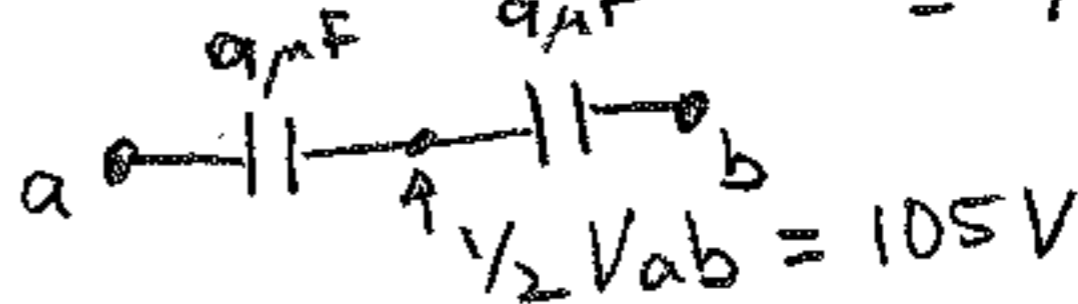
$$\text{so } V_{db} = 210V - 140V = 70.0V$$

$V_{ad} = V_{cb}$  &  $V_{db} = V_{ac}$  from symmetry of problem

so if  $V_a$  sits @ 210V, point d sits 140V below

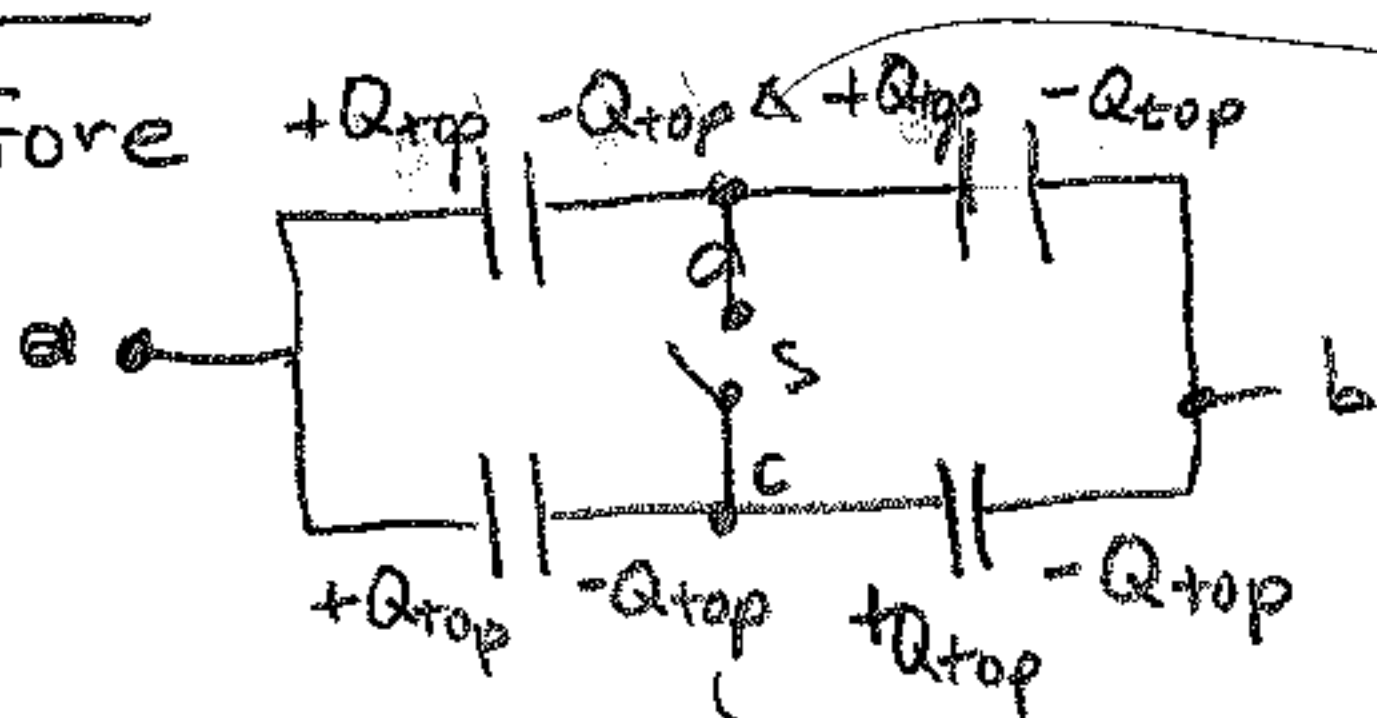
or  $V_d = 70.0V$  (means  $V_c = 140V$ )  $V_{cd} = V_c - V_d = 140V - 70.0V = 70.0V$

After switch S is closed, have



24.60

before



$$Q_{tot} = 0$$

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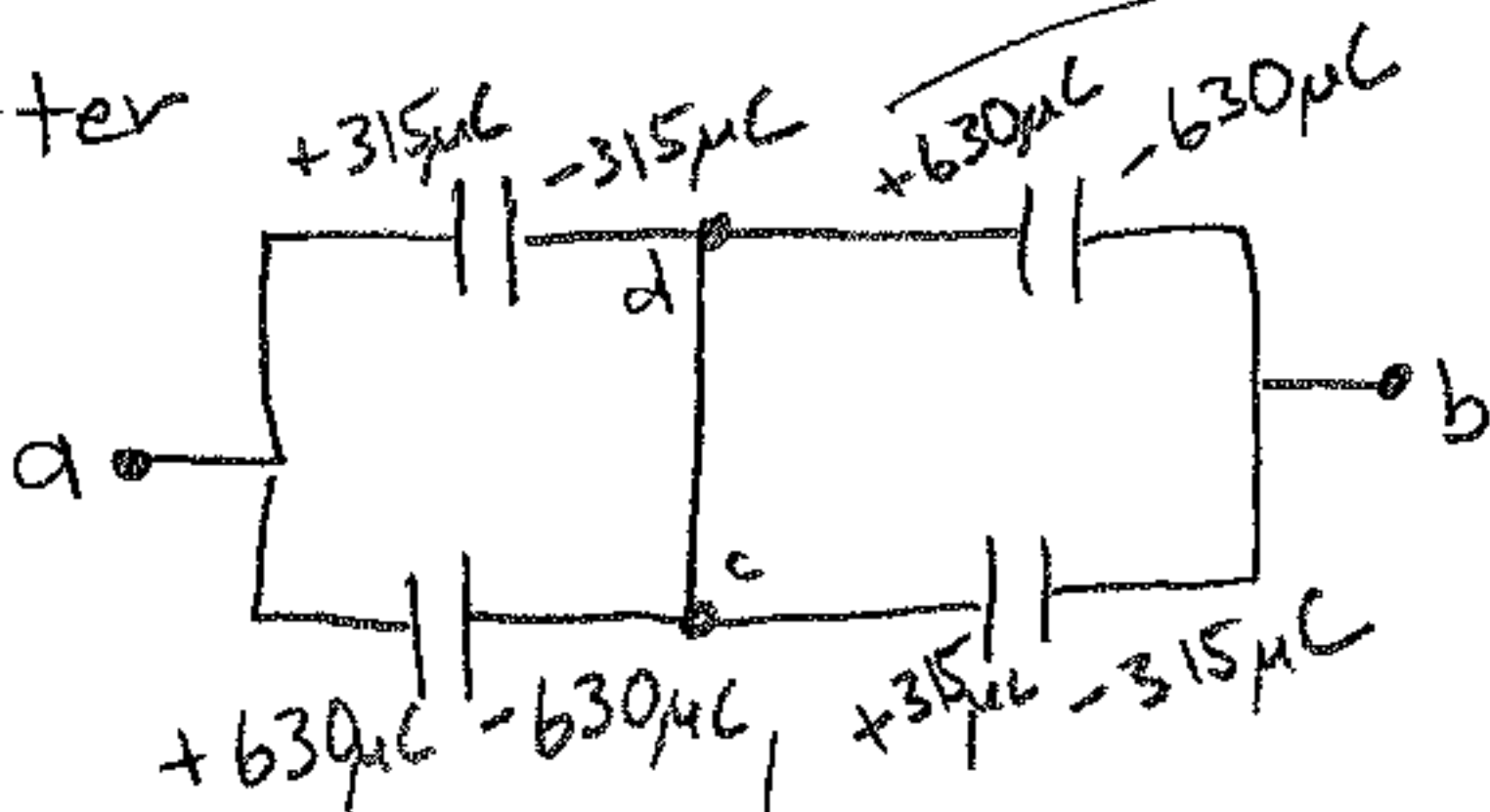
After  $Q$  across  $3\mu\text{F}$  capacitors =  $105\text{V}(3.00\mu\text{F})$

$$= 315\mu\text{C}$$

"  $6\mu\text{F}$  "

$$= 630\mu\text{C}$$

So After



$$Q_{tot} = 630\mu\text{C} - 315\mu\text{C}$$

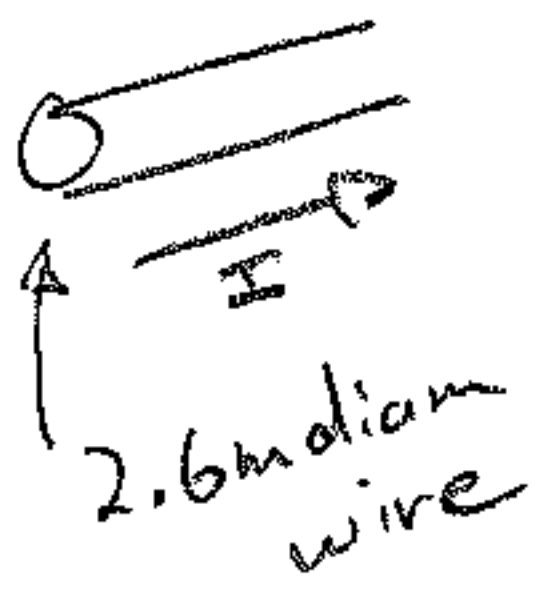
$$= 315\mu\text{C}$$

$$Q_{tot} = -630\mu\text{C} + 315\mu\text{C} = -315\mu\text{C}$$

so, looks like  $315\mu\text{C}$  flowed from  $c \rightarrow d$

25.2

420C get transferred in 80 min



$$I = \frac{\Delta Q}{\Delta t} = \frac{420\text{C}}{80\text{min} \cdot \frac{60\text{s}}{\text{min}}} = 0.0875\text{C/s}$$

Amp

$$J = nq v_d$$

$$v_d = \frac{J}{nq} = \frac{I/A}{nq} = \frac{(0.0875\text{C/s}) / (\pi (\frac{0.0026\text{m}}{2})^2)}{(\frac{5.8 \times 10^{28}}{\text{m}^3}) (1.6 \times 10^{-19}\text{C})}$$

$$= 1.8 \times 10^{-6}\text{m/s}$$

### Stretchable Resistor

$$R_0 = \frac{\rho l}{A}$$

In the stretch,  $V_0$  is constant

$$V_0 l = R A = (2l) A_{\text{new}}$$

before

$$A_{\text{new}} = \frac{A}{2}$$

$$R = \frac{\rho (2l)}{(A/2)} = 4 \frac{\rho l}{A} = 4R_0$$

### EMF

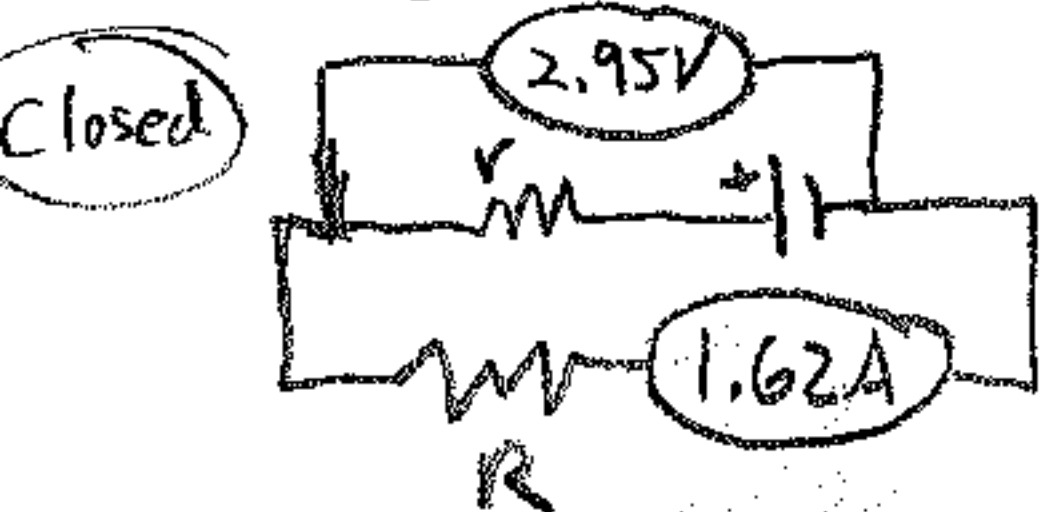
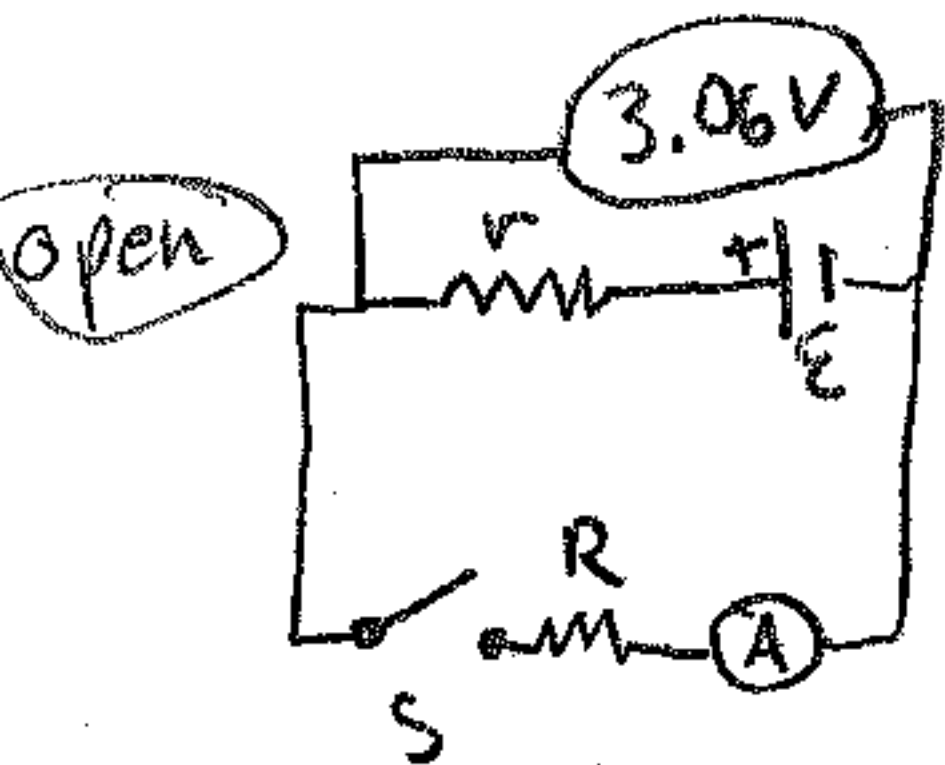
$\mathcal{E} = ?$  in the open config. very little current flows in  $r$ , so  $\Delta V$  on  $r$  is tiny  $\mathcal{E}$  is pretty close to 3.06V

$r = ?$  in closed position  $\Delta V$  across  $r$  drops 3.06V to 2.95V or  $\Delta V = 0.11\text{V}$ . Since 1.62A flows in the circuit

$$r = 0.11\text{V} / 1.62\text{A} = 6.79 \times 10^{-2}\Omega$$

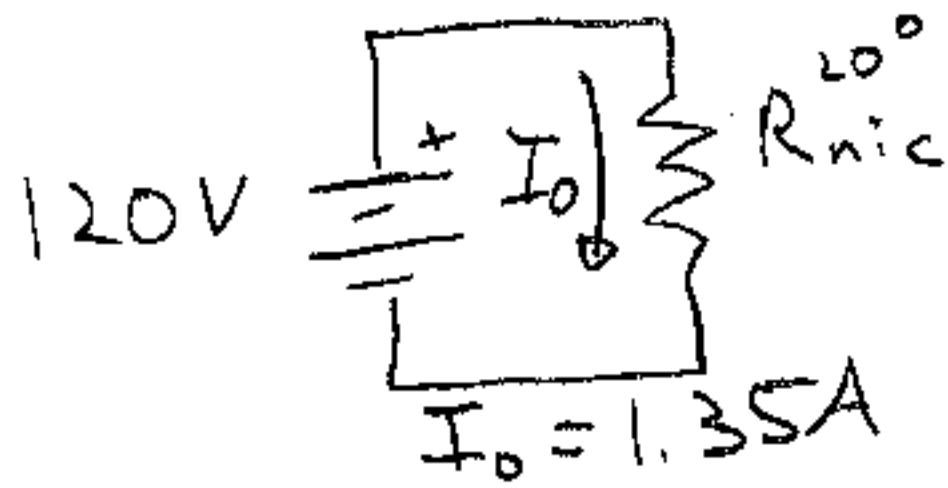
$R = ?$  well 2.95V goes across  $R$  so

$$R = 2.95\text{V} / 1.62\text{A} = 1.82\Omega$$



# 25.74 toaster

Initially @ 20°C



$$R_{nic}^{20^\circ} = \frac{120V}{1.35A}$$

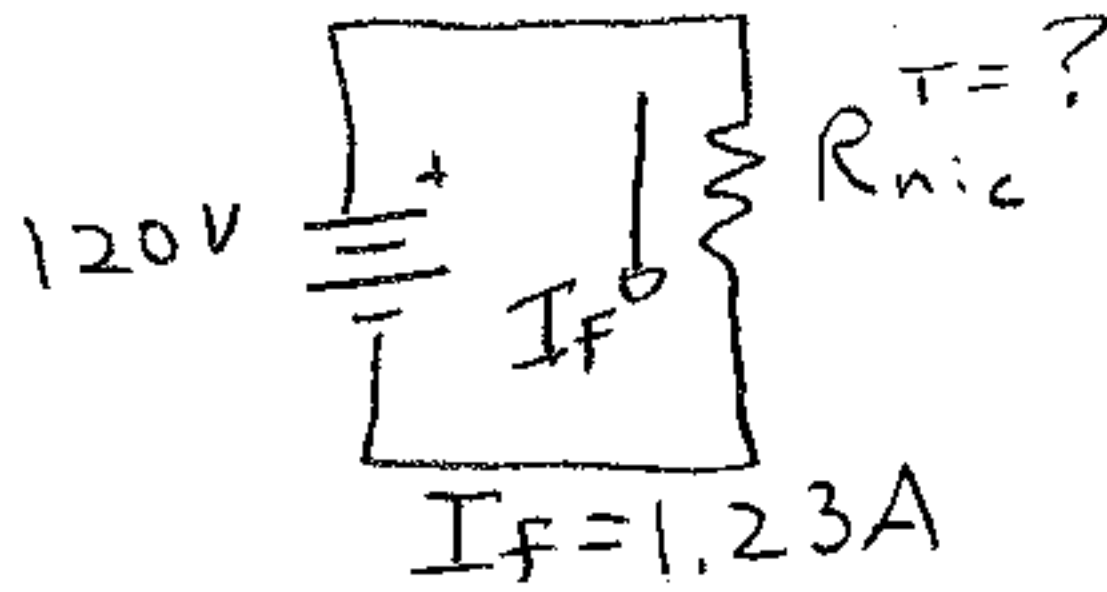
$$= 88.9\Omega$$

$$P_{nic}^{20^\circ} = I_0 V$$

$$= (1.35A)(120V)$$

$$= 162W$$

After a few secs



$$R_{nic}^{T=?} = \frac{120V}{1.23A} = 97.6\Omega$$

$$P_{nic}^{T=?} = (120V)(1.23A) = 147.6W$$

Assume volume change of nichrome is small

$$R_{new} = R_0 \alpha (T - T_0) + R_0$$

problem gives  $\alpha$  over the  $\Delta T$ , look @  $\Delta R$

$$R_{new} - R_0 = R_0 \alpha (T - T_0)$$

$$\frac{R_{new} - R_0}{\alpha R_0} = T - T_0 \quad T = \frac{R_{new} - R_0}{\alpha R_0} + T_0$$

$$T = \frac{97.6\Omega - 88.9\Omega}{(4.5 \times 10^{-4}/^\circ C)(88.9\Omega)} + 20^\circ C = 235^\circ C$$