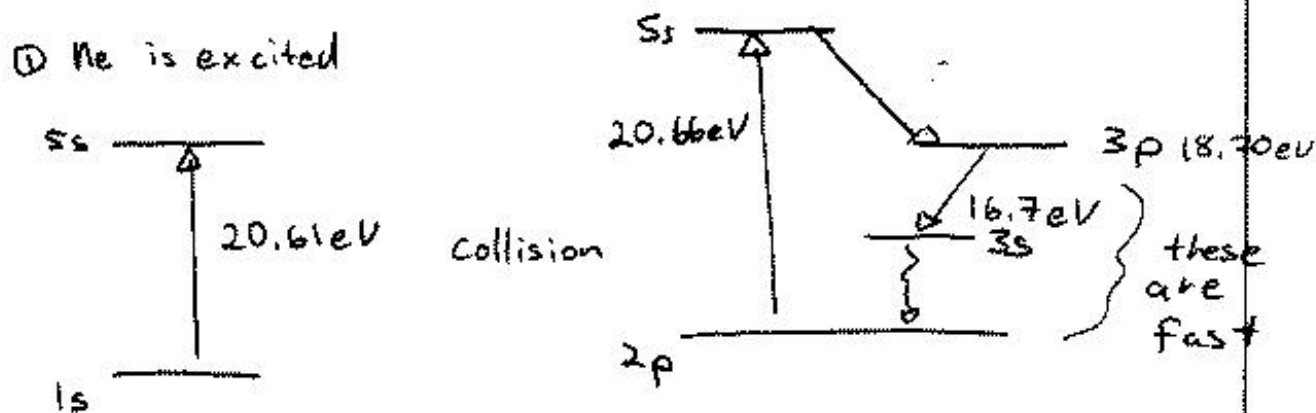


- how a HeNe laser works.
- ① Ne is excited by electrical discharge
 - ② Transfers this energy to He via a collision
 - ③ He emits photons via stimulated emission & we control the direction with mirrors
 - ④ He returns to the ground state



So what's with all this s, p stuff & why are there always s-p p-s like transitions when photons are emitted

Not ably in He, but other atoms too.

Turns out we need to modify our Bohr Picture. In quantum mechanics, angular momentum is pretty wierd stuff. We tend to think of it as stuff that rotates, in QM this is true, but it is also a question of symmetry. We've seen that the uncertainty principle tends to smear stuff out. Consider a pebble at the bottom of a bowl. This is the pebbles lowest energy state.

Now think about a super tiny pebble that gets kicked around by the uncertainty principle.

- This smeared out, spherically symmetric fuzz is hydrogen's lowest energy state

- Now suppose we give the pebble a horizontal kick, it starts to orbit, this is angular momentum, and a higher energy state

- Or suppose we give the tiny pebble some more energy, the fuzz will tend to spread out, this is also a higher energy

OK, so when we describe an atom's energy, we're going to need ways to describe states with and without angular momentum.

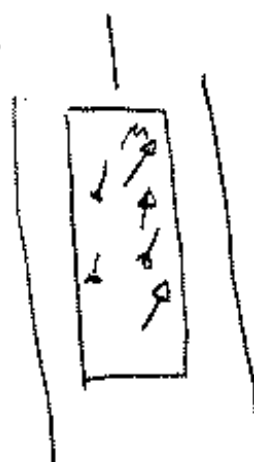
1) Is this real? Is it really angular momentum or just all fuzz?

Consider 2 experiments

1) Einstein - de Haas

turn on B

all μ 's align



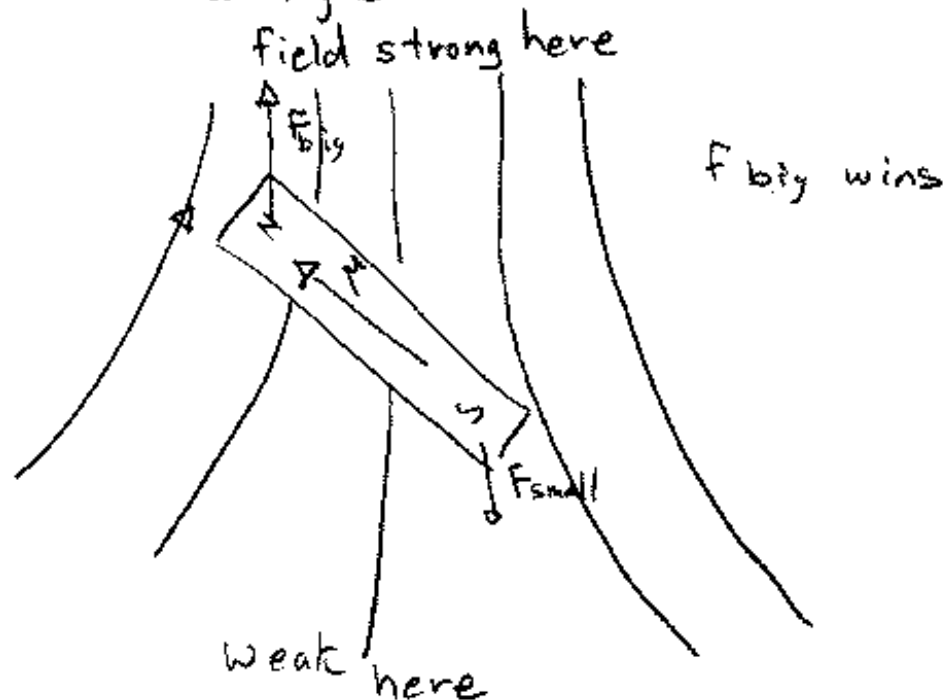
piece of iron in a magnetic field
all the little dipoles in iron are all over the place

$\rightarrow$ means all L in "same" direction = iron rotates

So this is really angular momentum

2) Put a beam of atoms in a non-uniform magnetic field (why non uniform)

think of a magnet

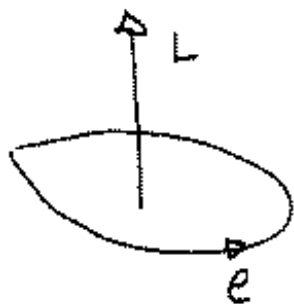


so what?

Quantum mechanics is really weird, turns out angular momentum is really quantized

Here's one reason why.

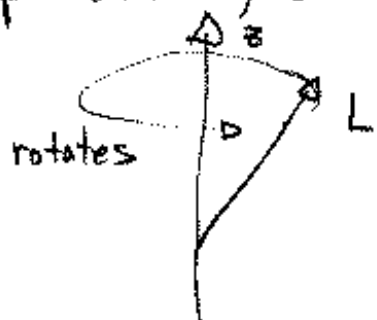
Consider an electron moving in an orbit



If we knew exactly where L pointed, we'd know $p_z = 0$ and $z = 0$ which can't be

$$\Delta z \Delta p_z \geq \frac{h}{4\pi}$$

so instead, we think about the L vector precessing around the z axis



so that we satisfy the uncertainty principle

the projections are quantized in units of $\left(\frac{h}{2\pi}\right)$ for an orbiting electron

now since L can rotate about $\pm z$ or $z=0$ (an x or y axis)

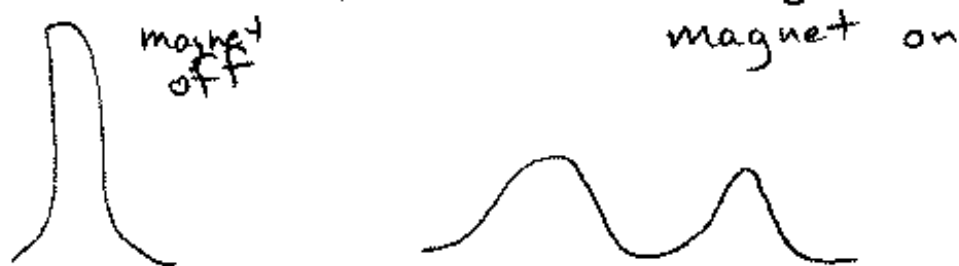
we say that the lowest L state actually has 3 possibilities

$$L_z = +\frac{h}{2\pi}, 0, -\frac{h}{2\pi}$$

So, if we run a beam of atoms through a magnetic field, we can determine which L_z is present, if this is truly what's happening.

This was done, and the results were surprising

① a split was seen, but it was too good



where is $L_z=0$?

Since silver was used, it was suggested to try this with something simpler, Hydrogen.

They found the same pattern.

Turns out that the electron carries an intrinsic angular momenta and it was screwing up all the nice theory.

$$S_z = \pm \frac{1}{2} \left(\frac{h}{2\pi} \right) \text{ only for an electron}$$

and this has no $S_z = 0$ projection.

This is called spin

- really, don't think there is a spinning electron
- but it is angular momentum all the same.

Now, it turns out that the most favorable transition are those where $\Delta L = 1$

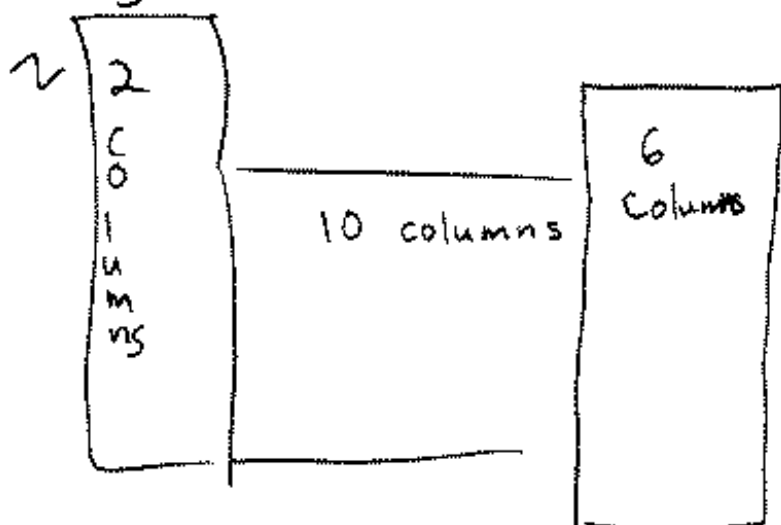
- This implies the photon has spin 1

When $\Delta L = 0$ you have to flip the spin of an electron to get a transition, & this is rarer.

- Still doesn't quite explain how the periodic table, ~~is~~ ϕ

- lets look at it a second

notice how its arranges
Hydrogen



as we go through the periodic table

- element get heavier
- elements get more electrons
- elements are neutral (need more mass than proton)
- some elements have similar chemical properties
- we said lowest energy is a spherically symmetric fuzzy state H
- next higher energy state (For a single electron) is to get some angular momentum
- but we don't have a bunch of electrons piling up in one giant fuzzy state

Pauli exclusion principle

- no 2 particles with $\frac{1}{2} \frac{h}{2\pi}$ spin can share the same state!

For 2 electrons

- so, lowest energy fuzzy state
is $s_z = +\frac{1}{2}$, $s_z = -\frac{1}{2}$ $L=0$ (2 states)

- when $L_z = \frac{h}{2\pi}$, 0 , $-\frac{h}{2\pi}$

each one of these can hold 2 electrons
(6 columns)

(He is where it is due to its
chemical properties)

$L_z = 2\frac{h}{2\pi}$, $\frac{h}{2\pi}$, 0 , $-\frac{h}{2\pi}$, $-2\frac{h}{2\pi}$
(10 columns)

or $L_z = m_l \frac{h}{2\pi}$ $m_l = -2, -1, 0, 1, 2$
 $= -2l, -l, 0, l, 2l$
and

orbital
quantum
number $l = n-1$
our old principle
quantum number

(electrons tend to fill the orbitals unpaired
1st) so, for $n=2$ energy state can have $l=1 \leq \begin{matrix} L_z=1 \\ L_z=0 \\ L_z=-1 \end{matrix}$
 $n=3$ $l=2$ $L_z = \begin{matrix} 2 \\ 1 \\ 0 \\ -1 \\ -2 \end{matrix}$, $l=1$ $L_z = \begin{matrix} 1 \\ 0 \\ -1 \end{matrix}$, $l=0$

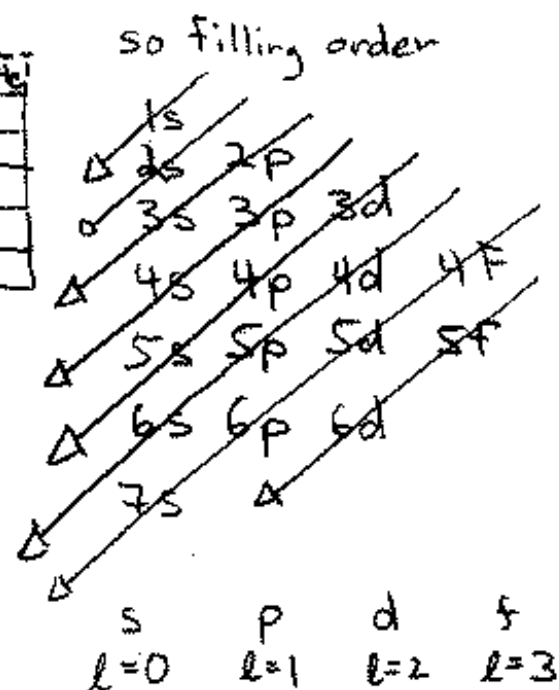
So, how would we completely fill the $n=3$ shell.

1) going to have to fill up the 4s (fuzzy) shell too

The layout of the periodic table will let you remember the order of filling

1s			
H He			
2s			2p
3s			3p
4s		3d	4p
5s		4d	5p
6s		5d	6p
7s		6d	

Funny stuff in here
start filling in f states



l is allowed as high as $(n-1)$

L_z goes $\pm l$ in integer steps
each L_z can have 2 electrons

So, to completely fill $n=3$, fill 1s, 2s, 2p, 3s, 3p, 4s, 3d

1s 0 0 $+\frac{1}{2}, -\frac{1}{2}$

2s 0 0 $+\frac{1}{2}, -\frac{1}{2}$

2p 1 0 $+\frac{1}{2}, -\frac{1}{2}$
 $+\frac{1}{2}, -\frac{1}{2}$
 $+\frac{1}{2}, -\frac{1}{2}$

3s 0 0 $+\frac{1}{2}, -\frac{1}{2}$

3p 1 0 $+\frac{1}{2}, -\frac{1}{2}$
 $+\frac{1}{2}, -\frac{1}{2}$
 $+\frac{1}{2}, -\frac{1}{2}$

4s 0 0 $+\frac{1}{2}, -\frac{1}{2}$

3d 2 0 $+\frac{1}{2}, -\frac{1}{2}$
 $+\frac{1}{2}, -\frac{1}{2}$
 $+\frac{1}{2}, -\frac{1}{2}$
 $+\frac{1}{2}, -\frac{1}{2}$
 $+\frac{1}{2}, -\frac{1}{2}$

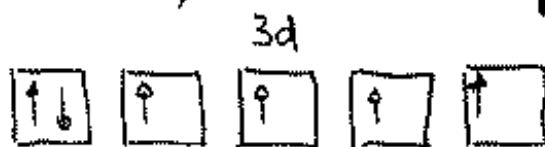
A total of 30 electrons,
this element is Zinc

How about a partially fill
3d, how do we arrange
the electrons?

Consider Iron, has $Z = 26$ (26 electrons)

has $1s, 2s, 2p, 3s, 3p, 4s$ filled & part of $3d$ filled, where do we put the e^- 's?

↑ indicates
spin
direction



or



book describes
Hund's Rule

(Fill electrons
unpaired)

both ok

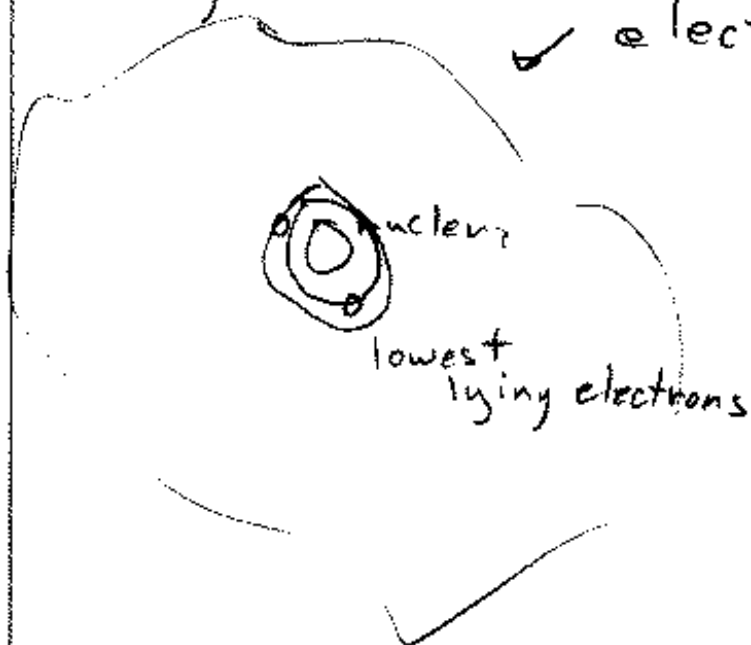
Book has this progressions

Z		$1s$	$2s$	$3p$
3	Li	↑↓	↑	
4	Be	↑↓	↑↓	
5	B	↑↓	↑↓	↑
6	C	↑↓	↑↓	↑ ↑
7	N	↑↓	↑↓	↑ ↑ ↑
8	O	↑↓	↑↓	↑↓ ↑ ↑
9	F	↑↓	↑↓	↑↓ ↑↓ ↑
10	Ne	↑↓	↑↓	↑↓ ↑↓ ↑↓

Hard to believe? Consider more evidence.

Suppose we have an atom with many electrons

✓ electrons outside



recall from gauss's Law, those inner electrons don't feel the effect of the outside electrons much, so they're really attracted to the nucleus

recall for Hydrogen

$$E_{\text{tot}} = -\frac{k_e e^2}{2r} \quad \frac{1}{r} = \frac{m_e (2\pi)^2}{n^2 h^2} k_e e^2$$

$$E_{\text{tot}} \propto Z^2 \quad \text{wow}$$

so that innermost electron is really held in there

Since there's another electron there though, there will be some repulsion
 So

$$E_0 \sim \underbrace{(Z-1)^2}_{Z_{\text{effective}}} - 13.6 \text{ eV}$$

charge of nucleus

if you can use this principle to determine other Energy states

$$E_n = \underbrace{(Z_{\text{eff}})^2}_p - \frac{13.6 \text{ eV}}{n^2}$$

n big more electrons inside

now, consider what happens if we knock out one of these inner electrons, there is a hole that can be filled up by an electron making a jump from a higher energy level to the lower one

$$E_{\text{higher}} = (Z - \underbrace{\left\{ \begin{array}{l} \# \text{ of electrons} \\ \text{in lower } n's \end{array} \right\}}_{\uparrow})^2 - \frac{13.6 \text{ eV}}{n^2}$$

and you see

don't forget one that's gone already!

$$E_{\text{photon}} = E_{\text{higher}} - E_0$$

These are characteristic of a material $\propto 1/n$

