

Creation of matter.

I did a little more research on neutron stars and the situation is nowhere near clear to me. Apparently, they aren't thought to exist beyond $3 M_{\text{sun}}$, and our estimate for a limit to the radius as that of a black hole is not too far off. A lot of the work requires a more general relativistic approach to the problem and a more accurate description of a stars interior.

We did notice something interesting in the lecture last time: $\frac{\# \text{ Neutrons}}{\text{total } \# \text{ atoms}} \sim 0.07$ in the sun

which gave us a ratio of $\frac{n}{p}$ of

$$\frac{0.07 (2n)}{0.93 (1p) + 0.07 (2p)} = \left(\frac{1}{7.6} \right)$$

assuming the rest is ^1H

The oldest rocks we've been able to find put the age of the solar system at about 5×10^9 y or about 1.5×10^{55} p-p interactions assuming 4×10^{26} W and 27 MeV/reaction. So if we consume 4 ^1H & create

$$N_{\text{H}} = 1.2 \times 10^{57} \text{ nucleons} = \# \text{ } ^1\text{H} + 4 \# \text{ } ^4\text{He} = \# \text{ } ^1\text{H} (1 + 0.3) \text{ now } \# \text{ } ^4\text{He} = \left(\frac{7}{93} \right) \left(\frac{N_{\text{H}}}{1.30} \right)$$

$$\# \text{ } ^4\text{He then} = 7 \times 10^{55} - 1.5 \times 10^{55} = 5.5 \times 10^{55}$$

so that gives us

$$\frac{\# \text{ Neutrons}}{\# \text{ atoms}} = \frac{5.5 \times 10^{55}}{1.2 \times 10^{57} - 4(5.5 \times 10^{55})} = 5.7\%$$

$$\frac{n}{p} = \frac{0.057(2)}{0.943 + 2(0.057)} = \frac{1}{9.3}$$

Which means that the neutrons in the sun probably came from some place else!

Suppose you created all the particles in a single huge event, what can you deduce?

⇒ probably took less than 10 minutes
(this is $t_{1/2}$ of a neutron)

otherwise neutrons would disappear

⇒ at one point it was hot enough and dense enough so that $\#n \sim \#p$

since we've seen $\#n = \#p e^{-1.3 \text{ MeV}/k_B T}$

type of stuff before.

So, how can we get an idea of what happened?

- 1) Assume we started out with a dense ball of stuff
- 2) Assume it expanded and cooled

tools

1) treat stuff as like any particle in a potential (even Hydrogen atom)

assume $E_{tot} = 0 = KE - (PE)$

$$\frac{1}{2} m \left(\frac{dr}{dt} \right)^2 = \frac{GMm}{r}, \quad m = \left(\frac{4}{3} \pi r^3 \right) \rho$$

$$\left(\frac{dr}{dt} \right)^2 = \left(\frac{4}{3} \pi r^3 \right) \rho \frac{G}{r}$$

$$= \frac{8}{3} \pi G \rho r^2 \quad (-kc^2)$$



and a correction

$$k \begin{cases} +1 & E_{tot} < 0, \text{ bound} \\ 0 & E_{tot} = 0 \text{ no limit} \\ -1 & E_{tot} > 0 \end{cases} ???$$

now, if we assume M is constant

$$\rho(r) = \frac{M}{\frac{4}{3} \pi r^3}$$

and

$$\left(\frac{dr}{dt} \right)^2 = 2 \frac{GM}{r}$$

$$\sqrt{r} dr = 2GM dt$$

$$\frac{2}{3} r^{3/2} = 2GM t$$

$$\text{or } r = (3GM t)^{2/3} \Rightarrow \left(\frac{dr}{dt} \right)^2 = \frac{2}{3} (3GM)^{2/3} t^{-1/3}$$

$$\text{or } \left(\frac{2}{3} \right)^2 \frac{(3GM)^{4/3}}{t^{2/3}} = \frac{8}{3} \pi G \rho (3GM)^{2/3} t^{-1/3}$$

$$t^2 = \frac{1}{6\pi G \rho M}$$

This says that after a long time, the universe is not too dense. (it's expanding)

When the universe was very dense and hot though, it acted more like a gas of photons. (lots of particle particle type annihilations going on) & we've dealt with a gas of photons before in the home work and in the class we found

$$\frac{\text{the number of photons}}{\text{Volume}} = (2.03 \times 10^7 / \text{m}^3 \text{K}^3) T^3$$

$$\text{or } T \propto \frac{1}{r}$$

$$\text{while the } \frac{\text{Energy}}{\text{Volume}} = (4.73 \times 10^3 \frac{\text{eV}}{\text{m}^3 \text{K}^4}) T^4$$

now, a way to deal with photons in a gravity field is to give them a "mass" E/c^2

$$\text{so we get } \rho_r = \frac{E}{V} \frac{1}{c^2} = (4.73 \times 10^3 \frac{\text{eV}}{\text{m}^3 \text{K}^4}) T^4$$
$$= (4.73 \times 10^3 \frac{\text{eV}}{\text{m}^3 \text{K}^4}) \left(\frac{\# \text{ photons}}{\frac{4\pi}{3} r^3} \right)^{\frac{4}{3}} = A / r^4$$

$$\text{so } \left(\frac{dr}{dt} \right)^2 = B \frac{1}{r^2} \quad \left(\text{From } \frac{8}{3} \pi G \rho_r r^2 \right)$$

$$r dr = \sqrt{B} dt$$

$$r^2 = 2Bt, \quad r = \sqrt{2B} t^{1/2}, \quad \left(\frac{dr}{dt} \right)^2 = (2B) \frac{1}{4t}$$

$$\frac{8}{3} \pi G \rho_r r^2 = \frac{8}{3} \pi G \rho_r (2B) t = 2B \frac{1}{4t}$$

$$t^2 = \frac{3}{32\pi G \rho_r}$$

or

$$t^2 = \frac{3c^2}{32\pi G (4.73 \times 10^3 \frac{\text{eV}}{\text{m}^3 \text{K}^4}) T^4}$$

$$T^4 = \frac{3c^2}{32\pi G (4.73 \times 10^3 \frac{\text{eV}}{\text{m}^3 \text{K}^4}) t^2}$$

$$T = \left(\frac{3 (3.0 \times 10^8 \text{ m/s})^2}{32\pi (6.67 \times 10^{-11} \frac{\text{Nm}^2}{\text{kg}^2}) (4.73 \times 10^3 \times 1.6 \times 10^{-19} \frac{\text{J}}{\text{m}^3 \text{K}^4})} \right)^{\frac{1}{4}} \frac{1}{\sqrt{t}}$$

$$= (1.5 \times 10^{10} \text{ s}^{1/2} \text{ K}) / t^{1/2}$$

Temperature is important, it tells us at what times certain things happen as the universe expands.

Temperature
 $k_B T \sim E_\gamma = 2 (940 \text{ MeV})$

whats happening
 Threshold to create
 $p\bar{p}$

$$\text{time} = 4.7 \times 10^{-7} \text{ s}$$

at this point, very short lived species are going to start to disappear (basically, everything with a c, s, t, or b quark is gone)

As things cool, no $p\bar{p}$ are made and the ones that are there annihilate. There is an imbalance though \bar{p} 's are left over.